Abstract - A new multiresolution (MR) M-ary differential chaos shift keying (DCSK) modulation scheme is proposed in this paper. It is a promising technique to provide different quality of services (QoS) for transmitted bits within a symbol according to their different bit error rate (BER) requirements based on the principle of non-uniformly spaced constellations. The new system not only is simple, but also provides better anti-multipath fading performance against various spreading factors, which inherits the advantages of the conventional DCSK system. Furthermore, the proposed scheme and its multicarrier version further increase spectral efficiency and use lower energy consumption at the same bandwidth as compared to the conventional DCSK and its multicarrier (MC-DCSK) system. Explicit BER expressions of the new system are derived and analysed over additive whiteGaussian noise (AWGN) aswell as multipath Rayleigh fading channels. All simulation results verify the prominent advantages of the new scheme and the accuracy of the new analytical approach.

Keywords— Multiresolution; M-ary DCSK; BER; AWGN channel; Multipath Rayleigh fading channel

I. INTRODUCTION

Conventional multiresolution (MR) modulation such as phase shift keying (PSK) and quadrature amplitude modulation (QAM) is a promising technique providing different quality of services (QoS) for transmitted bits according to their levels of importance. One advantage of the MR modulation is that it can support unequal error protection, i.e., a bit stream can be separated into several sub-streams with different levels of priority, including a high priority (HP) sub-stream and some lower priority (LP) sub-streams. The HP and LP data can be multiplexed and transmitted using an MR modulation in multimedia transmission digital broadcast simultaneous voice and multiclass data transmissions cooperative and relay systems and user scheduling in cellular networks. Another advantage is that it does not extend the bandwidth as compared to channel coding techniques which add redundancy into the transmitted data.

The reason for applying the multiresolution technique to chaos-based modulations lies in the significant advantages provided by chaotic signals. A chaotic signal has a unique characteristic of being sensitive to initial conditions, which allows the generation of a theoretically infinite number of uncorrelated signals. Owing to their wideband characteristics, chaotic signals have proven to be one of the natural candidates for spread-spectrum modulation schemes. Hence, chaos-based modulation is a kind of combining modulation with spread spectrum technology which has similar advantages as conventional spread-spectrum modulations, e.g. mitigation of fading channels, anti-jamming and low probability of interception (LPI) and secure communications. In addition, chaos-based sequences outperform Gold sequences in spread-spectrum communication systems.

The novel contributions of this are summarized as follows

1) A new multiresolution M-ary DCSK system is designed. It provides different QoS for transmitted bits within a symbol according to their different BER requirements.

2) In addition to the advantages of the conventional DCSK and MC-DCSK systems, the new system and its multicarrier version further increase the spectral efficiency and energy efficiency with the same bandwidth.

3) The analytical BER expressions of the proposed scheme over AWGN and multipath Rayleigh fading channels are derived and analysed.

II. M-ARY DCSK SYSTEM

In this chapter, we present the M-ary DCSK system, which is an extension of the 4-ary DCSK system, and then give the BER performance by simulations over AWGN channels.

A. Principle of DCSK System

The system based on M-ary DCSK modulation is shown in Fig. 1. First, the chaotic generator generates a chaotic reference signal $c_r$ which is transformed into another quadrature signal $c_q$ by using
Hilbert transform, thus two independent orthogonal chaotic signals are generated. For M-ary DCSK encoder (for the information signal), a constellation of chaotic signals can be generated as a linear combination of the quadrature signals $c_x$ and $c_y$, in the form of $m_s=a_s c_x + b_s c_y$, where the index $s$ identifies the symbol in the signal space with $s=1,\ldots,M$, and $a_s$ and $b_s$ present the real part and the image part corresponding to this symbol $s$, respectively (see Fig. 2 for 16-ary DCSK).

Similarly, to DCSK, in the first half symbol period the reference signal $c_x$ is transmitted and in the second half symbol period the information-bearing signal $m_s=a_s c_x + b_s c_y$ is sent. Hence, during the $l$-th symbol duration, the output of the transmitter is

$$s_k = \begin{cases} \sqrt{E_s/2} c_{x,k}, & k = 2(l-1)\beta+1, \ldots, 2(l-1)\beta+\beta \\ \sqrt{E_s/2} (a_{s} c_{x,k-\beta} + b_{s} c_{y,k-\beta}), & k = (2l-1)\beta+1, \ldots, 2l\beta \end{cases}$$

Where $E_s$ is denoted by symbol energy, $\sum_{k=1}^{\beta} c_{x,k} c_{x,k}=0$, $\sum_{k=1}^{\beta} c_{x,k}^2=1$, $\sum_{k=1}^{\beta} c_{y,k}^2=1$, $a_{s}^2+b_{s}^2=1$ and $2\beta$ is a spreading factor.

At the receiver, the noise-corrupted reference signal $c_x$ correlates the corrupted information-bearing signal, thus an observation value is obtained. Another observation value is computed by the corrupted reference signal, which is calculated by using the signal after Hilbert transform, and using the signal finally, the received symbol can be decided by the observation variables and using the decision boundaries and the received bits are reconstructed by the symbol/bits converter.

### B. Results

The simulated results are presented here to show the BER performance of M-ary DCSK modulation over AWGN channels. It was found that for small spreading factors $\beta < 16$, DCSK performs slightly better than 4-ary DCSK, while for large spreading factors, 4-ary DCSK outperforms DCSK. Hence, a large spreading factor is adopted in the simulation. On the other hand, the logistic map $x_{k+1}=1-2x_{2k}$ is used as the chaotic system. For the normalized chaotic signal with zero mean, the variance is equal to one.

Fig. 3 shows the BER performance curves of M-ary DCSK and MPSK-DCSK for spreading factor $\beta=60$ and $M=2, 4, 8, 16$, and $32$. For these two systems, it is observed that as the order $M$ becomes higher than 4, the BER performance decreases with an increase of the order. The best BER performance of
4-ary DCSK is obtained, which is different from the MPSK-DCSK system where PSK-DCSK and QPSK-DCSK have the same BER performance. Moreover, it is observed that the performance of M-ary DCSK is a little better than that of MPSK-DCSK, especially at a low order, M = 4 and 8. Finally, a better performance of the M-ary DCSK system is gained at the cost of a slightly higher complexity where the Hilbert transform operation is performed twice, as compared to the MPSK-DCSK system.

III. MULTIRESOLUTION M-ARY DCSK SYSTEM

In the case of MR 8-ary DCSK, the binary DCSK constellation represents the highest priority, which is represented by the “◦” symbol. The 4-ary DCSK constellation, i.e., the angle $\pi/2 - \theta_1$, $\theta_1 \leq \pi/4$, if the angle $\theta_1$ is larger than $\pi/4$, the information of the position is the HP bit) represents the second priority, denoted by the “∗” symbol. The angle $\theta_2$ denotes the third priority, which is marked by the “◦” symbol. Therefore, the binary DCSK modulation has the highest priority followed by 4-ary and 8-ary DCSK modulations. In other words, its principle is the same as the hierarchical PSK modulation. In Fig. 5, the MR 8-ary DCSK constellation also evolves from 4-ary DCSK modulation, which evolves from a binary DCSK modulation. Thus, we also refer this MR 8-ary DCSK constellation to as 2/4/8-ary DCSK, similarly to the hierarchical PSK modulation. In addition, it is noted that the “∗” symbols are only fictitious symbols, while the actual transmitted symbols are the “◦” symbols.

A. The Transmitter

In this system, the parallel information sequences of different QoS or different kinds of data services are first converted into a k-bit serial signal by a parallel-to-serial converter, which is converted into a symbol $s$ by using a bits/symbol converter. The symbol $s$ is encoded into the information signal by the M-ary DCSK encoder, i.e., $m_a = a_c + b_c$, where $a_c$ and $b_c$ are generated by the angle vector $\theta$. Finally, the chaotic reference signal and information signals $x_c(t) = \sqrt{E_s/2} \sum_{k=1}^{\beta} c_{k} h(t-kT_c)$ and $x(t) = \sqrt{E_s/2} \sum_{k=1}^{\beta} m_{i,k} h(t-kT_c)$, respectively are generated by pulse shaping, where $h(t)$ is the square-root-raised-cosine filter and $T_c$ is the chip time.

The transmitted signal of the MR M-ary DCSK can be expressed as

$$s(t) = x_c(t) \cos(2\pi f_c t + \phi_1) + x(t) \cos(2\pi f_c t + \phi_2)$$

where $\phi_1$ and $\phi_2$ denotes the phase angles of the carrier modulation. And the two modulated carriers are orthogonal.

B. The Receiver

The received signal is given by

$$r(t) = \sum_{l=1}^{L} \alpha_l (t - \tau_l) \otimes s(t) + n(t),$$

Where $L$ is the number of paths, $\tau$ is the channel coefficient and the path delay of the l-th path, respectively, $\otimes$ is the convolution operator, and $n(t)$ is a wideband AWGN with zero mean and power spectral density of $N_0/2$. Assume that $\alpha_l$ are independent Rayleigh distribution random variables. If the number of paths is equal to one, i.e. $L = 1$, with a unit channel coefficient $\alpha_l = 1$, then this is the AWGN case; otherwise, the Rayleigh fading case. This multipath Rayleigh fading channel model is commonly used in spread-spectrum wireless communication systems. To simplify the analysis, we only discuss L independent and identically-distributed Rayleigh fading channels, i.e. $E[|\alpha_l|^2] = E[|\alpha_1|^2] = \ldots = E[|\alpha_L|^2]$, while similar results are obtained for other cases. Thus, the probability density function (PDF) of the symbol-SNR $\gamma_c$ can be written as

$$f(\gamma_c) = \frac{2^{L^2 - 1}}{(L - 1)!\gamma_c^L} \exp \left(-\frac{2\gamma_c}{\bar{\gamma}_c}\right),$$

where $\bar{\gamma}_c$ is the average symbol-SNR per channel defined by
\[ \gamma_c = \frac{(E_s/N_0)E[\alpha_j^2]}{(E_s/N_0)E[\alpha_j^2]}, j \neq l, \]  
(4)

and

\[ \gamma_s = \left( \sum_{i=1}^{L} \alpha_i^2 \right) \frac{E_s}{N_0}, \]  
(5)

with \( \sum_{i=1}^{L} E[\alpha_i^2] = 1 \).

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C. Decisions

The decision vector is reconverted into the phase \( \omega = \arctan(z_a/z_b) \). This phase is then adopted for decoding the bit streams, i.e. identifying the most likely transmitted phase \( \theta \), so that one can get the information bits corresponding to this \( \theta \). The decision method is different from the M-ary DCSK, where individual bits instead of symbols are decoded. For example, in the case of MR 8-ary DCSK, shown in Fig. 5, the HP bit is “0” if the received phase is \( 0 < \omega < \pi \); otherwise bit “1” is identified. Similarly, the second priority bit is “0” in the right half plane; otherwise, it is “1”. However, the LP bits can be determined by the decision boundaries for which a computing method was given in [4]. For \( m \geq 3 \), the decision boundaries are necessary to calculate. Hence, the angle vector is known at the receiver.

IV. PERFORMANCE ANALYSIS OF MR M-ARY DCSK

A. Derivation of the CDF

The decision variables at the output of the correlators may be approximated as, respectively

\[ z_a \approx \sum_{k=1}^{L} \left( \sum_{i=1}^{L} \frac{E_s}{2} \left( a_i c_{x_k-b_f} + n_k \right) \right), \]  
(6)

\[ z_b \approx \sum_{k=1}^{L} \left( \sum_{i=1}^{L} \frac{E_s}{2} \left( a_i c_{y_k-b_f} + n_k \right) \right), \]  
(7)

The variances of (6) and (7) are computed as respectively.

\[ \text{Var}[z_a] = \sum_{i=1}^{L} \frac{E_s N_0}{2} \frac{\beta N_0^2}{4}, \]  
(9)

\[ \text{Var}[z_b] = \sum_{i=1}^{L} \frac{E_s N_0}{2} \frac{\beta N_0^2}{4}. \]  
(10)

Where \( n_k \) is an AWGN with zero mean and variance \( N_0/2 \), and \( n_k \) is the Hilbert transform of \( n_k \), which is also an AWGN with zero mean and variance \( N_0/2 \).

It can be seen that the decision variables \( z_a \) and \( z_b \) are independent Gaussian variables with means \( m_1 = \sum_{k=1}^{L} a_i c_{x_k-b_f} / 2 \) and \( m_2 = \sum_{k=1}^{L} a_i c_{y_k-b_f} / 2 \) respectively, and with the same variance \( \delta^2 = \sum_{k=1}^{L} \frac{E_s N_0}{4} + \frac{\beta N_0^2}{4} \).

Hence, the instance PDF is given by

\[ p(z_a, z_b) = \frac{1}{2\pi \delta^2} \exp \left( -\frac{(z_a - m_1)^2 + (z_b - m_2)^2}{2\delta^2} \right) \]  
(11)

Next, introduce the polar coordinates transformations of the decision vector \( (z_a, z_b) \) by

\[
\begin{align*}
V & = \sqrt{z_a^2 + z_b^2} \\
\Omega & = \arctan \left( \frac{z_b}{z_a} \right)
\end{align*}
\]

Fig 6. Signal vector perturbed by noise.
The cumulative distribution function (CDF) is given by

\[ F(\phi) = \int_{-\pi}^{\phi} p(\varphi) d\varphi, \quad -\pi < \phi < \pi \]

The CDF has the following characteristics:

\[
\begin{align*}
F(-\pi) &= 0, \\
F(\pi) &= 1, \\
F(0) &= 1/2
\end{align*}
\]

\[ p(\varphi) = p(-\varphi) \]

V. NUMERICAL RESULTS AND DISCUSSIONS

A. BER Comparisons with Conventional DCSK, M-ary DCSK and MC-DCSK

This is used to compare BER performance among the MR M-ary DCSK, conventional DCSK, and M-ary DCSK (including 4-ary DCSK). The spreading factor \( \beta \) is set to 160 and the priority vector is set to \( \theta = [\pi/3.5 \pi/15 \pi/40] \).

![Fig 7. BER performance comparisons between MR 16-ary DCSK with priority vectors \( \theta = [\pi/3.5 \pi/15 \pi/40] \), DCSK, 4-ary DCSK and 16-ary DCSK for spreading factor \( \beta = 160 \) over multipath Rayleigh fading channels.](image)

Fig 7 shows the BER performance comparisons among the MR 16-ary DCSK, conventional DCSK, 4-ary DCSK and 16-ary DCSK for spreading factor \( \beta = 160 \) over multipath Rayleigh fading channels.

Fig. 8 shows the BER performance comparisons among the MR 16-ary DCSK, conventional DCSK, 4-ary DCSK and 16-ary DCSK over multipath Rayleigh fading channels. It is observed that with the same bandwidth the transmission rate of the MR 16-ary DCSK system is four times than that of the DCSK system and it ensures that two bits be transmitted reliably as compared with the DCSK system. In addition, compared to the 4-ary DCSK, the MR16-ary DCSK obtains better performance at average BER of the high and second priority data and also increases the transmission rate. Furthermore, compared with the 16-ary DCSK, the MR16-ary DCSK can provide different reliability requirements.

![Fig 8. BER performance comparisons between MC MR 16-ary DCSK with priority vectors \( \theta = [\pi/3.5 \pi/15 \pi/40] \) and MC-DCSK for spreading factor \( \beta = 160 \) over multipath Rayleigh fading channels.](image)

To compare with the MC-DCSK, the proposed scheme is extended into the MC system. Here, the number of subcarriers is set to 4, the spreading factor \( \beta \) is set to 160 and the priority vector is set to \( \theta = [\pi/3.5 \pi/15 \pi/40] \).

![Fig 9. BER performance comparisons between the MC MR 16-ary DCSK and MC-DCSK over multipath Rayleigh fading channels.](image)

Fig. 9 shows the BER performance comparisons between the MC MR 16-ary DCSK and MC-DCSK over multipath Rayleigh fading channels. From the curves, it can be seen that, the proposed scheme offers higher data rate and lower energy consumption with the same bandwidth. In addition, every subcarrier can be equipped with different MR M-ary DCSK according to different requirements.

VI. CONCLUSION

A new simple generalized multiresolution M-ary DCSK system is designed. The new system enables simultaneous transmission of multiple sub-streams of the original stream with different levels of priority through the use of non-uniformly spaced constellations. Moreover, it offers better anti-multipath fading performance due to various spreading factors which inherit the advantages of the conventional DCSK system. Analytical BER expressions of the proposed system are derived over AWGN as well as multipath Rayleigh fading channels. Simulation results well match the analytical BER expressions, which demonstrate the accuracy of the proposed analytical method. These analytical BER expressions are dependent on the constellation size, the SNR, the spreading factors which ensure anti-multipath fading performance, and a constellation parameter which controls the relative message importance. Through adjusting the constellation parameter, the BER performance of different data priorities satisfies different service requirements without extending the bandwidth, which is different from channel coding. Compared to the DCSK and MC-DCSK, the proposed scheme and its multicarrier version further increase the spectral efficiency and energy efficiency with the same bandwidth.
REFERENCES


